



## ON IDEAL CONVERGENCE OF DOUBLE SEQUENCES IN NEUTROSOPHIC FUZZY $G$ -METRIC SPACES

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**Abstract.** The primary aim of this article is to introduce the concept of ideal convergence for double sequences in neutrosophic fuzzy  $G$ -metric spaces ( $NFGMS$ ) with order  $q$ . We explore the fundamental properties of this concept, analyze  $\mathcal{I}_2$ -Cauchy double sequences, and examine  $\mathcal{I}_2$  completeness in  $NFGMS$ . We provide examples of ideal convergent  $NFGMS$  and discuss their algebraic and topological properties. Additionally, we investigate the  $\mathcal{I}_2$ -limit and  $\mathcal{I}_2$ -cluster points of sequences. We also present  $\mathcal{I}_2$ -statistical convergence,  $\mathcal{I}_2$ -lacunary statistical convergence, strong  $\mathcal{I}_2$ -Cesàro summability, and strong  $\mathcal{I}_2$ -lacunary summability with order  $q$  in  $NFGMS$ , along with their associated properties.

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